

# Design and Test of FPGA-Based Direction-of-Arrival Algorithms for Adaptive Array Antennas

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*Abstract*—This paper presents the design and parametric testing of two FPGA-based, direction of arrival estimation algorithms (Bartlett and Minimum Variance Distortionless Response) for use in an adaptive array antenna system. The algorithms were implemented on a Xilinx Virtex-5 FPGA and tested using a test bed that emulates signals coming from an 8-channel, circular antenna head after being down converted to an intermediate frequency. The signals are digitized and fed to the FPGA using a custom A/D board. The algorithms were tested while sweeping the incident angle, power level, and single versus dual beams. This paper presents an overview of the digital implementation and the results of the parametric testing.<sup>1,2</sup>

The process of determining the angle of the incoming signal is called the *direction of arrival (DOA)* estimation. This is accomplished by processing the relative phases of the incident signal as observed by each of the antenna elements. The DOA estimation is then used to perform *Beamforming*, which is the process of creating the outgoing radiation pattern on the antenna array in the direction of the other communication node. The ability of the smart antenna to accurately determine the DOA of an incoming signal and resolve multiple transmitting nodes depends on the complexity of the signal processing algorithms used [2]. There are two main types of estimation techniques: (1) *spectral-based*, and (2) *parametric* [1-2]. In a spectral-based DOA, the spatial spectrum of the incident signal(s) is computed and the local maximas are used to find the angle of the incident wave front(s). In a parametric DOA, knowledge about the underlying data model is used to statistically predict the incident angle. Parametric algorithms tend to be more computationally intense than spectral-based DOA, but yield higher accuracy.

## TABLE OF CONTENTS

1. INTRODUCTION.....	1
2. SYSTEM DESIGN .....	2
3. DOA ESTIMATION ALGORITHMS.....	2
4. FPGA IMPLEMENTATION .....	3
5. TEST SETUP .....	4
6. DOA TEST RESULTS .....	5
7. CONCLUSION .....	5
ACKNOWLEDGMENTS .....	5
REFERENCES .....	8
BIOGRAPHY .....	8

## 1. INTRODUCTION

Adaptive array antennas, often called *smart antennas*, consist of a set of phased antennas that are able to detect the spatial location of a transmitting node and in turn form a directional beam pattern corresponding to the node's location. This type of directional communication system allows optimal use of transmitted power and reduces the effect of interference by reinforcing the signal(s) of interest and suppressing all others. Interfering sources can also be actively nullified using processing techniques to produce a more reliable communication link.

The use of Field Programmable Gate Arrays (FPGAs) in adaptive array antenna systems has received great interest recently due to the potential for increased accuracy and features in a smaller form factor. Advances in digital integrated circuit fabrication technology have made the idea of portable smart antenna systems a reality. This type communication system is of great interest to the military and aerospace community due to the need for small, lightweight radios with advanced features such as multiple beam tracking and noise nullification. FPGA-based processing has emerged as one of the most attractive technologies for complex DOA estimation due to the inherent flexibility of the hardware in addition to the ability to optimize the execution of the algorithm between hardware and software [11-15]. FPGAs allow time critical tasks such as Fast Fourier Transforms (FFTs) to be implemented in custom hardware while other less computationally intense operations can be performed in soft microprocessors. The ability to tailor the hardware implementation to the specific needs of the DOA algorithm makes FPGAs an attractive technology. Furthermore, the ability to implement all of the signal processing hardware on a single chip enables the practical deployment of smart antennas in portable communication devices.

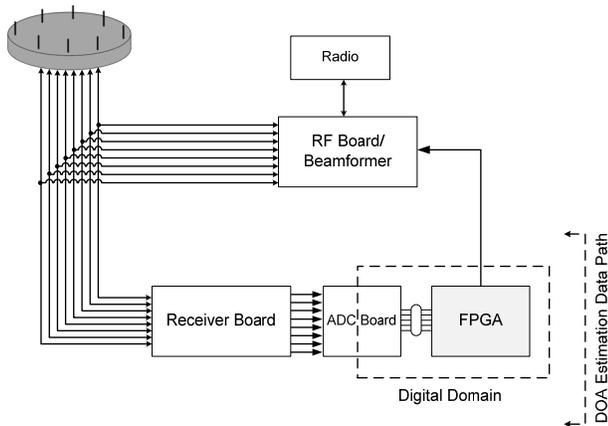
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<sup>2</sup>IEEEAC paper #1198, Version 7, Updated January 11, 2011  
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In this paper, we present the implementation and parametric testing of a set of DOA algorithms. A combination of hardware and software is used on the FPGA to deliver the highest performance while minimizing development time of new algorithms. The Bartlett and Minimum Variance Distortionless Response (MVDR) DOA algorithms are implemented and tested under a variety of input conditions. A laboratory test bed is used to emulate down converted signals which are digitized by the system and fed into the FPGA. This test setup enables the DOA algorithms to be evaluated while sweeping parameters of interest including single vs. multiple beams, signal-to-noise level, and different intermediate frequencies. All of the test data is recorded in the form of received power-out (dB) versus angle and the performance metrics are discussed.

## 2. SYSTEM DESIGN

A fully digital smart antenna system is being prototyped at Montana State University (MSU). The system is based on an 8-element circular antenna array. Figure 1 shows a block diagram of our system.



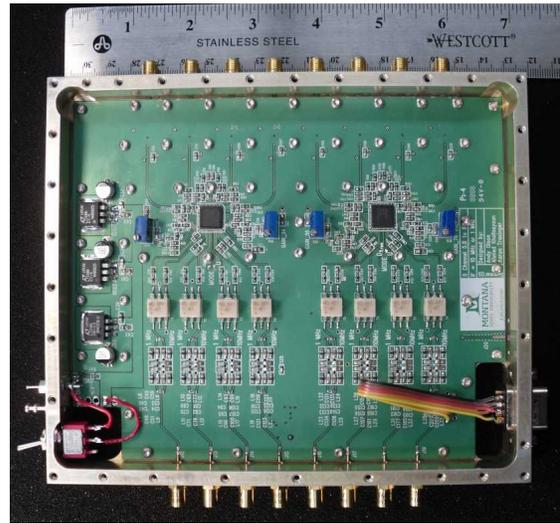
**Figure 1. Block diagram of fully digital smart antenna system.**

The circular antenna head is designed to receive signals on a carrier frequency of 5.8GHz. The array consists of 8x dipole antenna elements equally spaced around a 76mm circular ground plane and is shown in the following figure.



**Figure 2. 5.8GHz circular antenna head.**

A custom, 8-channel receiver board has been constructed at MSU that down converts the 5.8GHz signals to a programmable intermediate frequency between 1-10MHz. The receiver board is shown in the following figure.



**Figure 3. 8-Channel receiver board.**

A custom, 8-channel A/D board was constructed to sample the down converted signals at 25 MSa/s. The A/D board uses two, 4-channel Analog Devices AD9287 A/D converters which digitize the incoming signals and send the data to the FPGA in a serial manner using LVDS signal levels running at 200Mb/s. A Xilinx Virtex-5 FX70 FPGA on an ML507 evaluation board is used as the digital platform for the DOA estimation. The following figure shows the A/D board (left) connected to the Xilinx FPGA board (right).



**Figure 4. A/D board connected to the FPGA platform.**

## 3. DOA ESTIMATION ALGORITHMS

### *Bartlett DOA Estimation*

The Bartlett algorithm [18] is a Fourier spectrum analysis method. The goal is to find a set of weights  $w$  that maximize the received signal power. The  $m$ -element circular array receives signals from several spatially separated users. The received signals usually contain both direct path and multipath signals, which are most likely from different directions of arrival angles. Assume that the array response vector (also called steering vector) to a transmitted signal

$s_1(t)$  from a wave front arriving from an incident angle  $\varphi$  is  $\mathbf{a}(\varphi)=[1, a_1(\varphi), a_2(\varphi), \dots, a_{m-1}(\varphi)]^T$ , where  $a_i(\varphi)$  is a complex number denoting the amplitude gain and phase shift of the signal at the  $(i+1)$  antenna relative to the first antenna and superscript  $T$  is the transpose operator. For an  $m$ -element uniform circular array of radius  $\rho$ ,

$$\mathbf{a}(\varphi) = \left[ 1, e^{j\beta\rho \cos\left(\varphi - \frac{2\pi}{m}\right)}, \dots, e^{j\beta\rho \cos\left(\varphi - \frac{(m-1)\times 2\pi}{m}\right)} \right]^T \quad (1)$$

where  $\beta = 2\pi/\lambda$  is the wave number, the superscript  $T$  denotes the transpose operation. In a typical open space, we can ignore the multi-path signals. Thus the total signal vector received by the array can be written as:

$$\mathbf{x}(t) = \mathbf{a}(\varphi)s_1(t) + \mathbf{n}(t) \quad (2)$$

where  $\mathbf{n}(t)$  is the noise. If there are  $K$  sources that share the same frequency and time slot, then the signal received by the array is:

$$\mathbf{x}(t) = \sum_{k=1}^K \mathbf{a}_k(\varphi)s_k(t) + \mathbf{n}(t) \quad (3)$$

Assume that there is a signal coming from  $\varphi$ , the measurement of the Bartlett array output is:

$$\max_w E\{w^H \mathbf{x}(t) \mathbf{x}^H(t) w\} = \max_w E\left\{ |s(t)|^2 |w^H \mathbf{a}(\varphi)|^2 + \sigma^2 |w|^2 \right\} \quad (4)$$

where  $\sigma^2$  is the noise variance. The superscript  $H$  denotes to the conjugate transpose operation.

One obvious solution of Eq.1 is:

$$\mathbf{w}_B = \frac{\mathbf{a}(\varphi)}{\sqrt{\mathbf{a}^H(\varphi)\mathbf{a}(\varphi)}} \quad (5)$$

If  $\mathbf{a}(\varphi)$  is normalized, then the Bartlett weight vector is found to be:

$$\mathbf{w}_B = \mathbf{a}(\varphi) \quad (6)$$

This means that the Bartlett weight vector is equal to the incident wave spatial signature.

The covariance matrix of an array signal for a limited length is:

$$\hat{\mathbf{R}} = \frac{1}{T} \sum_{t=1}^T \mathbf{x}(t) \mathbf{x}^H(t) \quad (7)$$

where  $T$  is the sampling time. The output power spectrum of Bartlett method can be described as:

$$P = \frac{\mathbf{a}^H(\varphi) \hat{\mathbf{R}} \mathbf{a}(\varphi)}{\mathbf{a}^H(\varphi) \mathbf{a}(\varphi)} \quad (8)$$

If  $\mathbf{a}(\varphi)$  is normalized, then the output power spectrum is found to be:

$$P = \mathbf{a}^H(\varphi) \hat{\mathbf{R}} \mathbf{a}(\varphi) \quad (9)$$

Solving equation 9 for a given  $\varphi$  will give the power level observed at that observation angle of the antenna head. By solving across the entire  $0^\circ \rightarrow 359^\circ$  degree range of incident angles, the algorithm can estimate the angle of incoming wave by looking at angles with the most received power. The resolution of the algorithm depends on how many times  $P(\varphi)$  is solved for between  $0^\circ \rightarrow 359^\circ$ . For this work, we sweep  $\varphi$  in increments of  $1^\circ$ .

#### MVDR DOA Estimation

The MVDR algorithm (also called *Capon*) [3] is also a Fourier spectrum analysis method, but with the exception that the output power spectrum is given by:

$$P = \frac{1}{\mathbf{a}^H(\varphi) \hat{\mathbf{R}}^{-1} \mathbf{a}(\varphi)} \quad (10)$$

By performing an inverse on the covariance matrix, the side lobes and side nulls traditionally observed in the Bartlett output power spectrum can be eliminated.

## 4. FPGA IMPLEMENTATION

Within the FPGA, the time critical tasks are accomplished using hardware cores generated by the Xilinx ISE tools. Custom VHDL was developed for the A/D board interface. The sampling system was designed to sample 1024 samples across 8-channels at a rate of 25MSa/s and store the data into a 1024x8 block memory on the FPGA. On our system, receiver board only provides the positive frequencies to the A/D board so the sampled data consists of only real components. In order to convert the sampled data into a complex baseband equivalent received signal vector, a Hilbert transform is performed. A Hilbert transform consists of three steps: (1) an FFT; (2) a cancellation of negative frequency components; and (3) an iFFT. This transform is performed in hardware using a combination of custom VHDL and Xilinx Cores for the FFT/iFFT. The sampling and Hilbert transformation yield the  $\mathbf{x}(t)$  in equation 3.

The DOA estimation is performed in software within a MicroBlaze soft processor. It was discovered during implementation that performing the DOA estimation on the entire 1024 samples led to false peaks associated with the starting and stopping of the sampler. For our design, we perform the DOA estimation on the middle 512 samples.

The FPGA first normalizes the sampled data by removing any DC offset and dividing each channel by its standard deviation. The covariance matrix,  $\mathbf{R}$ , is then computed giving the results for equation 7.

The steering vector for the 8-channel circular antenna head,  $a(\phi)$  is calculated offline for the precision desired by the DOA system. For our system, we choose  $\phi=1$  degree due to memory constraints on the MicroBlaze. The steering vector is stored as a constant table.

For Bartlett DOA, the output power is calculated using equation 8. For MVDR DOA, an additional matrix inversion is performed on the covariance matrix ( $R^{-1}$ ) prior to the output power calculation in equation 9. The results of the estimation are stored in a  $360 \times 32$  memory element that can be used later by the smart antenna system.

### 5. TEST SETUP

In order to test just the digital DOA estimation, a test bed was created that could drive controlled signals directly into the A/D board. Four Tektronix AFG3022 dual channel arbitrary/function generators were used. These four generators were controlled using *National Instruments* Labview to generate 8-signals which are phased according to the desired incident angle to the antenna head. A Labview interface was created to control the generators. A Matlab GUI was created that offloaded the power vs. angle data from the FPGA. The following figures show the block diagram of the test bed, photos of the laboratory setup, and screenshots of the signal generator control GUI and FPGA interface GUI.

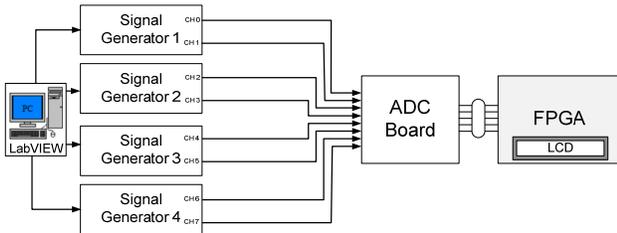


Figure 5. Block diagram of DOA test bed.

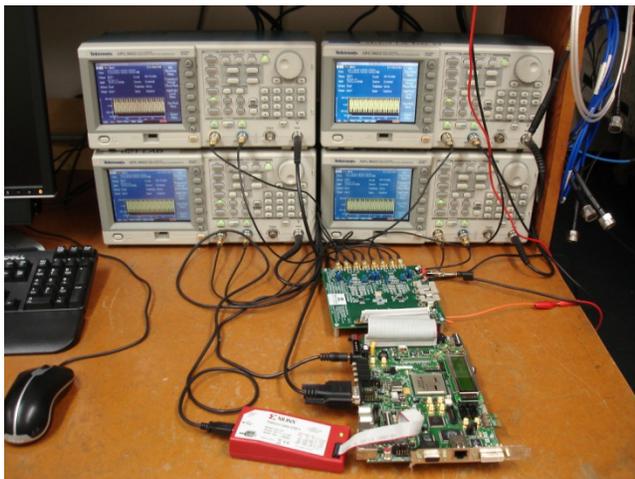


Figure 6. Laboratory setup.

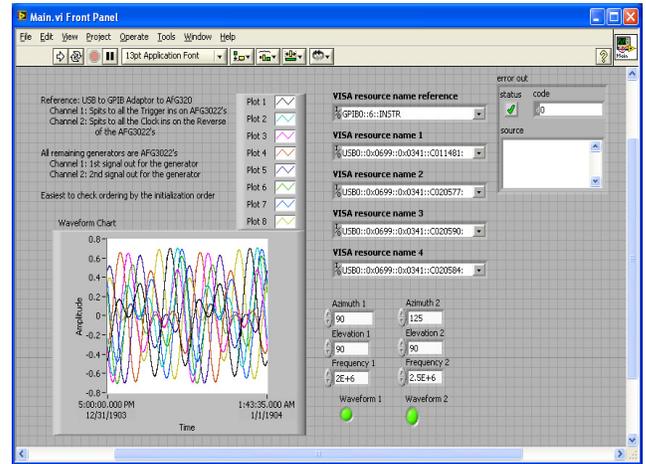


Figure 7. Screenshot of GUI to control the signal generators.

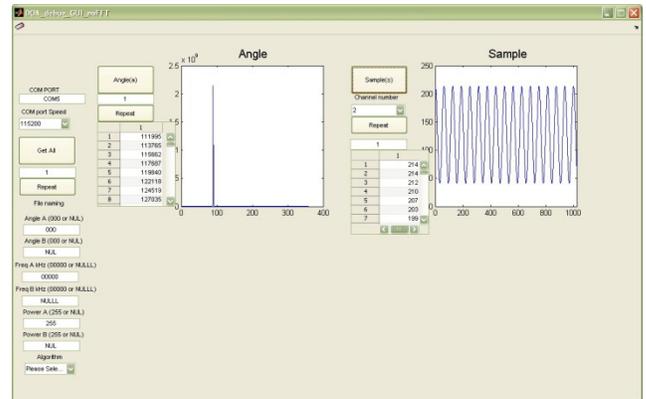


Figure 8. Screenshot of GUI that interfaces to the FPGA to receive output power vs. angle for the DOA estimation.

Both DOA algorithms were tested under a variety of conditions. First, an single incident beam was swept from  $0^\circ$  to  $359^\circ$  and the resultant power output vs. angle was recorded from the FPGA. This measurement was performed for both a full power signal and a minimum power signal. The full power signal consisted of a  $1V_{pp}$  signal. This represented the full dynamic range of the 8-bit A/D converters used in our system. The minimum power signal consisted of a  $20mV$  signal, which was the smallest level that the signal generators could output. This minimum signal amplitude corresponded to 3-bits of digitization in the A/D converter.

Next, two angles were sent into the DOA system. One angle was fixed at  $180^\circ$  and the other was swept from  $0^\circ$  to  $359^\circ$ . Again, both full power and minimum power signals were used.

## 6. DOA TEST RESULTS

### *Bartlett Test Results*

Figure 9 show the results of the parametric testing of the Bartlett DOA estimation. Subplot (a) shows the power-out spectrum of the DOA algorithm for a single beam arriving at the antenna head from an angle of  $90^\circ$ . In this plot, both the full power signal (1Vpp) and minimum power signal (20mVpp) responses are shown. There is a noticeable difference in the noise floors between the full and minimum signal strengths, but both responses' minimums occur at -20dB or below. Subplot (b) shows the same power-out spectrum information for an incident angle of  $270^\circ$ . Subplots (c) and (d) show the power-out spectrums for two incident beams with (c) showing incident angles of  $90^\circ$  and  $180^\circ$  and (d) showing incident angles of  $180^\circ$  and  $270^\circ$ . In all plots, the largest measured output power corresponds to the incident angles driven into the system by the signal generators which verify the functional operation of the hardware.

A spectrograph can be used to observe the output power for a full sweep of incident angles. The abscissa in the spectra plots is the *set angle*, which represents the angle of the incoming wave front generated by the signal sources. The ordinate of the spectra plots is the detected power vs. angle spectrum. This spectrograph represents 360 different measurements displayed in one plot. The dark red color in this plot represents the highest power while the dark blue represents the lowest. Subplot (e) shows the DOA spectra for the full signal swing (1Vpp) measurements while subplot (f) shows the spectra for the minimum signal swing (20mV). Both of these subplots show the output power as a single incident beam is swept from  $0^\circ$  to  $359^\circ$  in steps of  $1^\circ$ . Subplot (g) shows the spectra for two beams at full signal swing (1Vpp) with one being held at a  $180^\circ$  incident angle while the other is swept from  $0^\circ$  to  $359^\circ$  in steps of  $1^\circ$ . Subplot (h) show the same two beam spectra as (g), but with minimum signal swings (20mVpp).

When using the DOA output power in a smart antenna system, the data is typically processed to find the peak magnitude. The angle at which the peak power occurs is assumed to be the angle of arrival for an incident wave front. Subplot (i) shows the angle of the peak power (called *detected angle*) for the full signal swing spectra from subplot (e). Subplot (j) shows the angle of the peak power for the minimum signal swing spectra from subplot (f). Subplots (k) and (l) show the detected angle for two beams corresponding to (g) and (h) respectively. Subplots (k) and (l) graphically show where DOA estimation algorithms cannot discern between the two beams. Subplots (m), (n), (o), and (p) show the error between the set angle and the detected angle for subplots (i), (j), (k), and (l). For a perfect DOA estimation, the result should be that each detected angle matches the set angle and there is no error. Subplot (m) indicates that the DOA estimation corresponded to the set angle driven into the system when using a full power

signal level (1Vpp). Subplot (n) shows that there were two incident angles for the 20mV signal level where the DOA estimation produced a detected angle that was  $1^\circ$  different than the set angle. Note that our system was designed to have a resolution of  $1^\circ$ . Subplots (o) and (p) shows that the two-beam error becomes severe between  $140^\circ$  and  $230^\circ$ . This error indicates that the DOA estimation cannot discern between the two angles when the incoming wave fronts are within  $40^\circ$  of each other.

In all cases, the Bartlett performance matched ideal simulations. This verified that the FPGA-based implementation of the algorithm was correct and that limitations to the performance of the estimation were inherent in the algorithm itself.

### *MVDR Test Results*

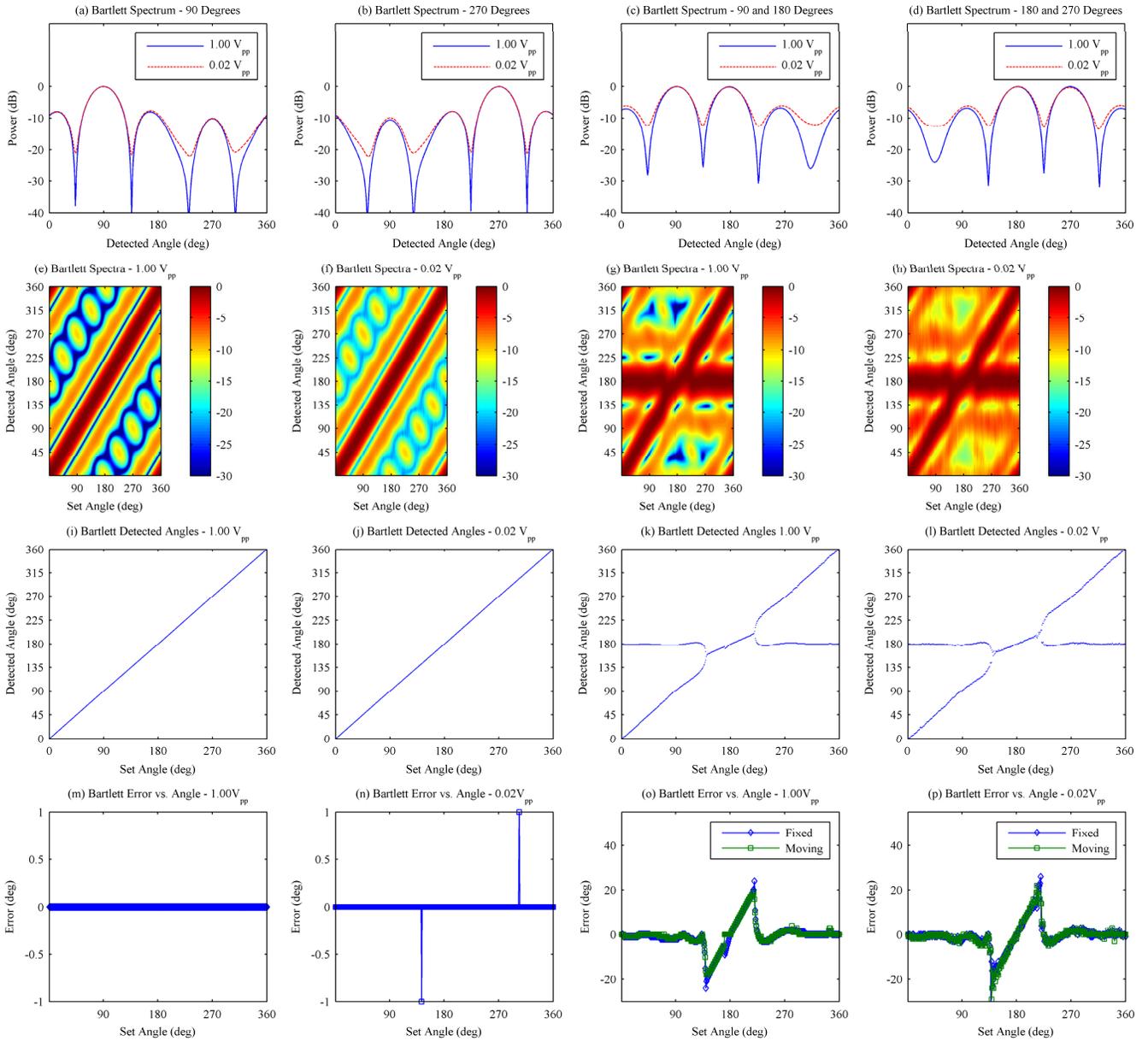
Figure 10 shows the results of the parametric testing of the MVDR DOA estimation. All of the subplots in this figure were produced under the same stimulus as in the Bartlett testing. These plots clearly show the increased accuracy of the MVDR algorithm. Most noticeable are the reduction in side lobes that are characteristic of the Bartlett algorithm. This not only results in a lower noise floor, but allows the algorithm to discern between multiple incoming waves with higher precision. Subplots (o) and (p) indicate that MVDR can detect the presence of multiple beams as close as  $5^\circ$  to each other. The drawback in the MVDR algorithm is the increased computation time to perform the inverse of the covariance matrix.

## 7. CONCLUSION

This paper presented the design and testing of two DOA estimation algorithms implemented on an FPGA. The Bartlett and MVDR DOA algorithms were tested under a variety of conditions including incident angle, single vs. multiple beams, and full vs. minimum power levels. A test bed was constructed to drive controlled signals into the digital DOA system in order to verify the functional operation of just the algorithms. Both implementations were verified to produce the functionally correct results. As expected, the MVDR algorithm outperformed Bartlett in both accuracy, multiple beam detection, and signal to noise ratio.

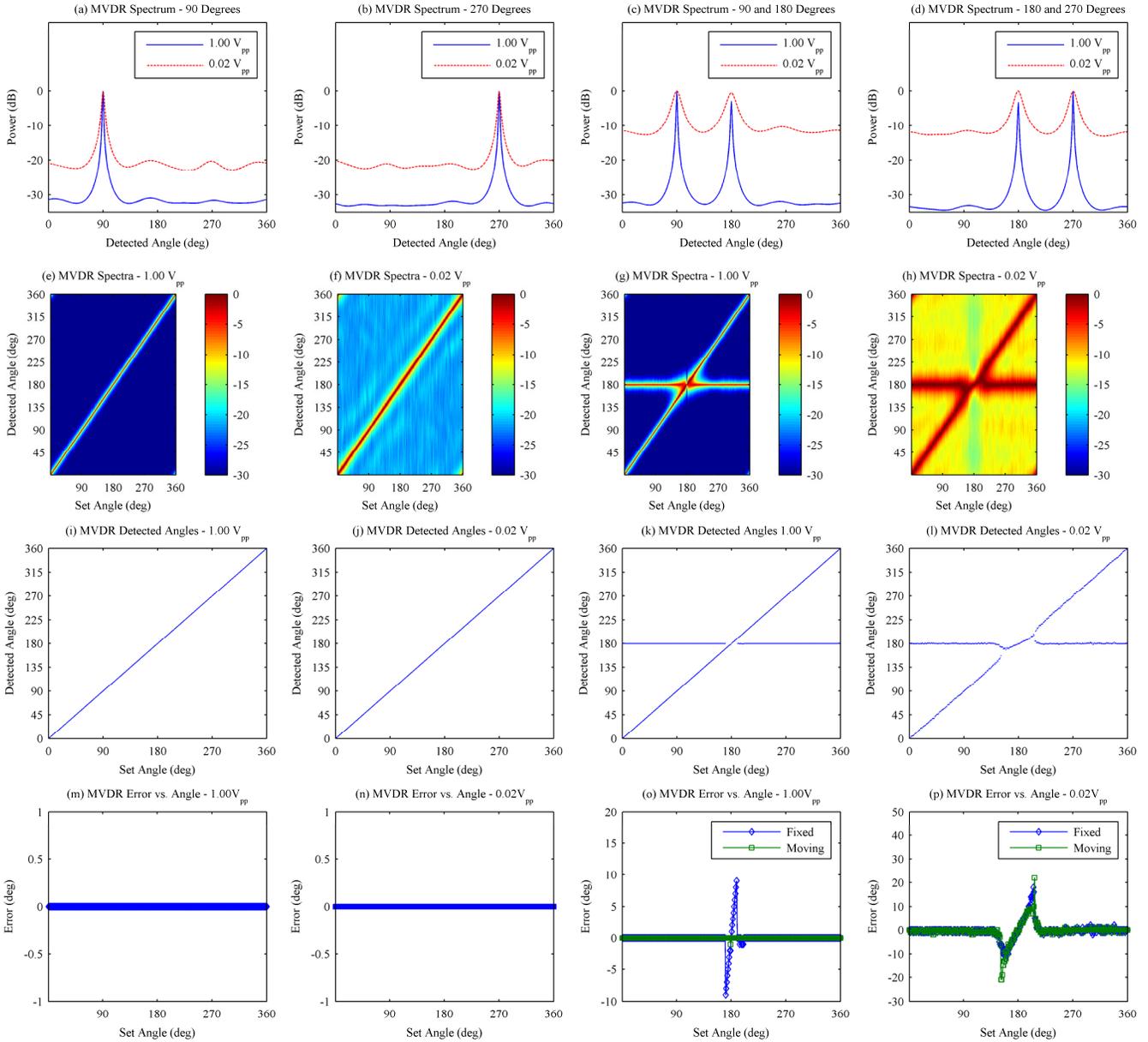
### ACKNOWLEDGMENTS

The authors would like to thank Advanced Acoustic Concepts (AAC) for support of this work.



**Figure 9. Parametric testing results of the FPGA-based, Bartlett DOA estimation.**

- (a) Power-out spectrum of a single incoming wave front at  $90^\circ$  for both a  $1V_{pp}$  and  $0.02V_{pp}$  signal level
- (b) Power-out spectrum of a single incoming wave front at  $270^\circ$  for both a  $1V_{pp}$  and  $0.02V_{pp}$  signal level
- (c) Power-out spectrum of two incoming wave fronts at  $90^\circ$  and  $180^\circ$  for both a  $1V_{pp}$  and  $0.02V_{pp}$  signal level
- (d) Power-out spectrum of two incoming wave fronts at  $180^\circ$  and  $270^\circ$  for both a  $1V_{pp}$  and  $0.02V_{pp}$  signal level
- (e) Power-out spectra of a single,  $1V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (f) Power-out spectra of a single,  $0.02V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (g) Power-out spectra of two,  $1V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$
- (h) Power-out spectra of two,  $0.02V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$
- (i) Peak detected power-out of a single,  $1V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (j) Peak detected power-out of a single,  $0.02V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (k) Peak detected power-out of two,  $1V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$
- (l) Peak detected power-out of two,  $0.02V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$
- (m) Error between set angle and detected angle of a single,  $1V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (n) Error between set angle and detected angle of a single,  $0.02V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (o) Error between set angle and detected angle of two,  $1V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$
- (p) Error between set angle and detected angle of two,  $0.02V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$



**Figure 10. Parametric testing results of the FPGA-based, MVDR DOA estimation.**

- (a) Power-out spectrum of a single incoming wave front at  $90^\circ$  for both a  $1V_{pp}$  and  $0.02V_{pp}$  signal level
- (b) Power-out spectrum of a single incoming wave front at  $270^\circ$  for both a  $1V_{pp}$  and  $0.02V_{pp}$  signal level
- (c) Power-out spectrum of two incoming wave fronts at  $90^\circ$  and  $180^\circ$  for both a  $1V_{pp}$  and  $0.02V_{pp}$  signal level
- (d) Power-out spectrum of two incoming wave fronts at  $180^\circ$  and  $270^\circ$  for both a  $1V_{pp}$  and  $0.02V_{pp}$  signal level
- (e) Power-out spectra of a single,  $1V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (f) Power-out spectra of a single,  $0.02V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (g) Power-out spectra of two,  $1V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$
- (h) Power-out spectra of two,  $0.02V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$
- (i) Peak detected power-out of a single,  $1V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (j) Peak detected power-out of a single,  $0.02V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
- (k) Peak detected power-out of two,  $1V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$
- (l) Peak detected power-out of two,  $0.02V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$
- (m) Error between set angle and detected angle of a single,  $1V_{pp}$  incoming wave front while sweeping the incident angle from  $0^\circ$  to  $359^\circ$
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- (p) Error between set angle and detected angle of two,  $0.02V_{pp}$  incoming wave fronts with one incident at  $180^\circ$  and the other incident angle swept from  $0^\circ$  to  $359^\circ$

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