

Table of Fourier Transforms and Properties		
	Time Domain $f(t)$	Fourier Domain
definitions	<i>definition of Inverse Fourier Transform</i> $f(t) = \int_{-\infty}^{\infty} F(f) e^{j2\pi f t} df$	<i>definition of Fourier Transform</i> $F(f) = \int_{-\infty}^{\infty} f(t) e^{-j2\pi f t} dt$
unit impulse	$\delta(t)$	1
unit step	$u(t)$	$\frac{1}{2} \delta(f) + \frac{1}{j2\pi f}$
exponential	$e^{j2\pi f_o t}$	$\delta(f - f_o)$
rectangular pulse	$\text{rect}(t)$ (see definitions below)	$\text{sinc}(f)$ (see definitions below)
sine	$\sin(2\pi f_o t)$	$\frac{1}{2j} (\delta(f - f_o) - \delta(f + f_o))$
cosine	$\cos(2\pi f_o t)$	$\frac{1}{2} (\delta(f - f_o) + \delta(f + f_o))$
Fourier Series	$\sum_{n=-\infty}^{\infty} C_n e^{jn2\pi f_o t}$	$\sum_{n=-\infty}^{\infty} C_n \delta(f - nf_o)$
Table of Fourier Transform Properties		
Linearity	$Af_1(t) + Bf_2(t)$	$AF_1(f) + BF_2(f)$
n <sup>th</sup> Derivative	$\frac{d^n f(t)}{dt^n}$	$(j2\pi f)^n F(f)$
Frequency shift	$e^{j2\pi f_o t} f(t)$	$F(f - f_o)$
Time Shift	$f(t - t_o)$	$e^{-j2\pi f t_o} F(f)$
Time Scaling	$f\left(\frac{t}{a}\right)$	$ a F(af)$
Time reversal	$f(-t)$	$F(-f)$
Convolution in time	$\int_{-\infty}^{\infty} f_1(\tau) f_2(t - \tau) d\tau$	$F_1(f) F_2(f)$
Convolution in frequency	$f_1(t) f_2(t)$	$\int_{-\infty}^{\infty} F_1(f') F_2(f - f') df'$
<p>Function Definitions: <math>\text{rect}(x) = \begin{cases} 1, &amp;  x  \leq \frac{1}{2} \\ 0, &amp;  x  &gt; \frac{1}{2} \end{cases}</math> , <math>\text{sinc}(x) = \sin(\pi x)/\pi x</math></p>		