Influence of Transmission Impairments on the OSMOSIS HPC Optical Interconnect Architecture

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Abstract—We examine the impact of transmission impairments on the performance of the optical supercomputer interconnect architecture, initially proposed in the context of the optical shared memory supercomputer interconnect system (OSMOSIS) project. We study two versions of the aforementioned optical interconnect that differ in terms of the number of semiconductor optical amplifiers (SOAs) used as ON–OFF gates. For practical reasons related to packet arbitration, the size of the crossbar switch of the optical interconnect in this study is limited to 64 ports. The switch is based on a broadcast-and-select architecture and employs DWDM in conjunction with 10 Gb/s intensity modulation/direct detection per wavelength channel. We show, both by experiment and by simulation, that the minimization of the number of SOAs in the optical switch by taking advantage of the cyclic routing capability of optical arrayed waveguide multiplexers/demultiplexers leads to negligible performance deterioration compared to conventional wavelength-space switches that are prohibitive slower and do not use any inherent gain properties like in OSMOSIS.

Index Terms—Optical interconnects, semiconductor optical amplifiers (SOAs), switching

I. INTRODUCTION

THE performance of high-performance computing (HPC) systems (i.e., supercomputers and computer clusters) experiences a tenfold increase every four years [1], it is expected that exascale HPC systems will be developed by 2020 [2], [3]. Until then, to satisfy the requirements of emerging, bandwidth-demanding applications for HPC systems, it is necessary to gradually replace the inefficient, conventional electronic interconnects with optical ones. For instance, two representative examples of state-of-the-art PetasFlops (PF) supercomputers (BlueWaters [4] and POWER7-IH [5]) use optical interconnects for inter-rack communication.

The optical shared memory supercomputer interconnect system (OSMOSIS) project [6] proposed an optical interconnect architecture for high bandwidth, low latency, cost-effectiveness, and scalability. The OSMOSIS optical interconnect uses electronics for scheduling and routing and optics for switching and transmission. Its basic building block is a two-stage, broadcast-and-select, 64 × 64 optical crossbar switch fabric for synchronous, fixed-size optical cell switching. The latter is accomplished through semiconductor optical amplifiers (SOAs), acting as ON–OFF gates [6]. The main advantage of the OSMOSIS architecture is that it performs nanoscale switching, as opposed to active optical cables, which are used for dedicated point-to-point links between pairs of nodes. In this sense, OSMOSIS is superior to the currently used optical active cable technology in terms of sharing resources. Nevertheless, the cost of the OSMOSIS architecture is still prohibitive for commercial HPC systems, due to the large number of ON–OFF gates. The problem is exacerbated as the throughput of the interconnect must eventually grow to accommodate exascale traffic.

An economically viable, multistage alternative design of the original two-stage OSMOSIS [6] crossbar switch fabric architecture, targeted at the minimization of the number of SOAs, was recently proposed [7]. More specifically, the multistage N × N optimum interconnect alternative design proposed in [7] can reduce the number of ON–OFF gates from 2N√N, which are required in the original two-stage OSMOSIS architecture [6], down to asymptotically N log N, where N is the number of nodes to be interconnected.

In a preliminary study [8], we experimentally investigated the performance of the multistage optimized crossbar switch fabric employing polarization division multiplexing (PDM) quadrature phase-shift keying (QPSK) modulation and coherent in-line detection. In a more recent publication [9], we have showed that the economically viable optimized optical switch fabric performs almost equally well to the original one when using conventional intensity modulation/direct detection (IM/DD).

Elaborating on the work of [9], in this paper, we assess the physical layer performance of the optimized 64 × 64 three-stage OSMOSIS optical switch fabric and compare it to its two-stage original counterpart, both experimentally and by simulation. In particular, we evaluate the impact of SOA nonlinearities, optical filter concatenation, and amplified spontaneous emission (ASE) noise accumulation, on the performance of both interconnect architectures, using 10 Gb/s IM/DD serial optical transmission. Simulation and experiment show that the optimized, cost-efficient OSMOSIS crossbar switch fabric performs almost as well as the original one, despite the fact that, in the former, optical signals travel through more concatenated SOAs.

The remainder of this paper is organized as follows. In Section II, we compare the original and the optimized crossbar switch designs and describe the simulation block diagrams.

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used to evaluate their performance. Their performance is also assessed through experimental measurements using the setup described in Section III. An itemized account of the penalties due to various transmission effects is presented in Section IV. Details of the simulation models are given in Appendix A. An analytical calculation to justify the results shown in Section IV is presented in Appendix B.

II. OPTICAL INTERCONNECT ARCHITECTURES

In this section, we describe the originally proposed [6] and the optimized [7], 64 × 64 OSMOSIS optical interconnect architectures and their simplified simulation block diagrams. Both architectures use fixed-wavelength transmitters and discretely tunable, direct-detection receivers. However, they differ in the organization of the transmitters into different multiplexing hierarchies and the number of stages in the discretely tunable receivers that perform the selection of the desired channel.

A. Original OSMOSIS Architecture

In the original OSMOSIS architecture [6], depicted in Fig. 1, the 64 transmitters are partitioned into eight sets. The transmitters of each set are assigned eight equidistant carrier frequencies. The frequency allocation plan for this scheme is shown as an inset in Fig. 1. Frequency reuse is employed among different transmitter sets. Each transmitter in Fig. 1 comprises a continuous wave (CW) laser. The output signal from each CW laser is first amplified by an erbium-doped fiber amplifier (EDFA) and then is intensity modulated by a 10 Gb/s, non-return-to-zero (NRZ), pseudorandom Binary Sequence (PRBS), using a Mach–Zehnder modulator (MZM). All channels are synchronized in time. Each set of eight channels is wavelength division multiplexed (WDM) on a different fiber; the WDM signal reaches the second EDFA (acting as a booster amplifier) without any power variation among the eight channels. The maximum power variation of the channels at the output of the second EDFA is less than 1 dB, due to the spectral tilt in the EDFA gain profile. We assume that the SOA gain has a parabolic shape around the SOA gain peak. Uniform channel placement around the peak of the SOA's gain curve minimizes power variation. More specifically, individual channels exhibit a maximum power variation of approximately 0 dB, both at the input and at the output of the first SOA, as well as at input of the second SOA. The SOAs work in the linear regime, close to their saturation point. Their input saturation power is $P_{\text{sat}} = 4 \text{ dBm}$ (see Fig. 9 in Appendix A). Additional ASE noise is loaded to the signal to vary the optical signal-to-noise ratio (OSNR) and estimate the error probability. After the second selection stage, the desired wavelength is filtered by an optical Gaussian filter at the entrance of the optically amplified receiver.

Fig. 1. Block diagram of the originally proposed 64 × 64 OSMOSIS optical interconnect architecture [6]. Eight identical sets of eight equidistant carrier frequencies are multiplexed and transmitted over eight separate fibers. On each receiver card, there are two discretely tunable stages. Eight SOAs are used per selection stage (i.e., 16 SOAs per receiver card). (Symbols: EDFA = Erbium-doped fiber amplifier, SOA = Semiconductor optical amplifier, AWG MUX/Demux = Arrayed waveguide grating multiplexer/demultiplexer, Tx = Transmitter, Rx = Receiver).

For the simulation, the channel spacing $\Delta f$ is 100 GHz. More specifically, the carrier frequencies of the transmitted channels are 192.1–192.8 THz (corresponding to wavelengths 1554.94–1560.60 nm). They are placed uniformly around the peak of the SOA gain, at 1557.77 nm, so they experience only a small gain variation due to the nonuniform SOA gain profile. The CW laser average power is set to $-3 \text{ dBm}$ per channel. The EDFA before the MZM has 17 dB gain to compensate for losses in the MZM and the consecutive multiplexer (MUX). The WDM signal reaches the second EDFA (acting as a booster amplifier) without any power variation among the eight channels. The maximum power variation of the channels at the output of the second EDFA is less than 1 dB, due to the spectral tilt in the EDFA gain profile. We assume that the SOA gain has a parabolic shape around the SOA gain peak. Uniform channel placement around the peak of the SOA's gain curve minimizes power variation. More specifically, individual channels exhibit a maximum power variation of approximately 0 dB, both at the input and at the output of the first SOA, as well as at input of the second SOA. The SOAs work in the linear regime, close to their saturation point. Their input saturation power is $P_{\text{sat}} = 4 \text{ dBm}$ (see Fig. 9 in Appendix A). Additional ASE noise is loaded to the signal to vary the optical signal-to-noise ratio (OSNR) and estimate the error probability. After the second selection stage, the desired wavelength is filtered by an optical Gaussian filter at the entrance of the optically amplified receiver, with an equivalent noise bandwidth $B_0 = 34 \text{ GHz}$ [10].

B. Optimized OSMOSIS Architecture

The proposed optimized 64 × 64 optical interconnect architecture is presented in Fig. 2. The 64 transmitters are partitioned into four sets. The transmitters of each set are assigned 16 carrier frequencies. Frequency reuse is employed among different transmitter sets. The frequency allocation plan is shown in the inset of Fig. 2. The 16 carrier frequencies are grouped into four wavebands in sets of four, occupying an aggregate bandwidth of
2.7 THz. Guard bands facilitate waveband multiplexing/demultiplexing. The carrier frequencies span from 192.1 to 194.8 THz (corresponding to the wavelength range 1538.98–1560.60 nm). The channel spacing within a waveband $\Delta f$ is 100 GHz. The signals of each transmitter set are WDM on a separate optical fiber and broadcasted to all 64 receiver cards using 1:64 star couplers. The discretely tunable receivers use three selection stages for choosing a fiber, a waveband, and a wavelength channel, respectively. The wavelength allocation is done in a way that the periodicity of arrayed waveguide grating (AWG) multiplexer/demultiplexer (MUX/DMUXs) is exploited. More specifically, to reduce the number of SOAs in the proposed architecture, we use periodic MUX/DMUXs at the wavelength selection stage, with a free spectral range of $\text{FSR} = 8 \Delta f$. After the third selection stage, additional ASE noise is loaded to the signal in order to assess the transmission performance. At the entrance of the optical preamplified receiver, the desired wavelength is filtered by an optical Gaussian filter, similar to the one used in the original architecture.

### III. Experimental Setup

The experimental setup used to measure the performance of the aforementioned, optimized 64 × 64 optical switch fabric is depicted in Fig. 3. Due to lack of resources, nine semiconductor lasers on the transmitters’ side emulate all 16 wavelength channels per fiber shown in Fig. 2. For the same reason, the wavelength channel distribution with reference to the SOA’s gain peak is not the same in the simulation and in the experiment. More specifically, eight DFB lasers, with carrier frequencies spaced by 100 GHz, are used to represent the first two wavebands, $W_1-W_2$. The carrier frequencies span from 192.469 to 193.563 THz (corresponding to the wavelength range 1548.808–1557.608 nm). A ninth (tunable) semiconductor laser, with eight times the nominal average power of a single WDM channel, located at the frequency slot $f_{21.5} = 192.164$ THz ($\lambda_{21.5} = 1556.608$ nm), is used to represent the remaining two wavebands $W_3-W_4$ [see Fig. 3(a)]. The nominal and the experimentally implemented frequency allocation plans are shown in Fig. 3(b), (gray and blue arrows, respectively). The CW optical signals from all nine lasers are initially combined and preamplified by an EDFA. Then, the WDM signal is modulated using a single MZM modulator by a 10 Gb/s, NRZ, amplitude shift keying (ASK), $2^7-1$ PRBS. This way, time-aligned, identical wavelength channel bit sequences are generated. This corresponds to the worst case scenario for studying the impact of cross-gain modulation (XGM) due to SOAs. Subsequently, the signal is first amplified again using a booster EDFA, and then it goes through a variable optical attenuator with 18 dB loss, which emulates the 1:64 star coupler of the actual OSMOSIS architecture. On the receiver side, the WDM signal passes through three cascaded selection stages that employ SOAs as ON–OFF gates. More specifically, the WDM signal originating from any one of the four fibers can be chosen by the first selection stage, composed of a SOA, and a 4:1 combiner. The second selection stage is used to select the desired waveband. Due to lack of resources, it consists of a 100 GHz AWG MUX with interconnected arms to emulate the 400 GHz AWG required in the proposed architecture [7], a second SOA, and an attenuator of 6 dB to emulate another 400 GHz AWG MUX, not available in the lab. The use of a 100 GHz AWG with interconnected arms as a substitute for the 400 GHz AWG is not completely accurate, and results in the filtering of some out-of-channel ASE noise in each waveband.
before amplification. Nevertheless, we anticipate that the performance would be affected only slightly by this substitution. The same approach was employed also in [9]. Finally, the desired channel is selected via a third wavelength selection stage, which consists of a pair of conventional AWG MUX/DMUX, with 100 GHz spacing, and four SOAs in our experiment, only the three SOAs that work in the ON state [i.e., black SOA boxes in Fig. 3(a)] are used. All SOAs have a 3 dB bandwidth of 90 nm, a small-signal gain of 15 dB, a gain peak at 1490 nm, a high input saturation power of approximately 4 dBm (see Appendix A, Fig. 9), and a low polarization-dependent gain (PDG) of < 0.2 dB.

A second experimental setup, described in detail in [6], is used for evaluating the performance of the original OSMOSIS optical switch fabric. Its description is omitted here for brevity. Only, the implemented frequency allocation plan for that experiment is shown in Fig. 3(b). The carrier frequencies span from 192.866 to 193.563 THz [corresponding to the wavelength range 1548.808–1554.408 nm (see Fig. 3(b)]. Another laser with three times the nominal average power of a single WDM channel, located at the frequency slot $f_{55} = 193.015$ THz ($\lambda_{55} = 1553.208$ nm), is used to represent the lasers not available in the lab [see Fig. 3(b)].

IV. SIMULATION AND EXPERIMENTAL RESULTS

In this section, we evaluate the performance of both optical interconnect architectures using the raw BER as a criterion. In practice, the raw BER is reduced by using additional forward error correction coding and/or automatic repeat request protocol. We investigate the impact of SOA nonlinear effects, such as self-gain modulation (SGM), XGM, and four-wave mixing (FWM), optical bandwidth narrowing due to AWG concatenation, and ASE noise accumulation on the performance of the optical interconnect. We show that the optimized architecture performs well, almost equally to the original one, despite the stricter limitations imposed by the additional stage of SOAs.

We define here three reference systems used in the following sections for performance comparison: 1) by the term “ideal system,” we refer to the one described in [11], where optical signal is assumed to be distortionless and the ASE noise is filtered at the IM/DD receiver by a brickwall optical BPF and an integrate-and-dump low-pass filter (LPF) (in the absence of a polarizer); 2) the term “back-to-back” refers to a hypothetical scenario where the selection stages of the receiver [i.e., gray boxes in Fig. 3(a)] are omitted; and 3) the term “single-channel transmission” refers to the hypothetical case where only one wavelength, i.e., the one that experiences the best or worst performance, is transmitted through the OSMOSIS architecture. A commercially available software tool (VPI Transmision-Maker), enhanced with custom-made modules in MATLAB for OSNR measurements, was used for carrying out the simulations shown [12]. Moreover, Mathematica software was also used to validate the SOA model.

A. Overview

The BER is assessed as a function of the received OSNR for each of the transmitted wavelengths, both by experiment and simulation. The final results are shown in Figs. 4 and 5 for the original and the optimized OSMOSIS architecture. Wavebands $W_1 - W_4$ ($\lambda_0 - \lambda_2^f$) were investigated by simulation while $W_1 - W_2$ ($\lambda_0 - \lambda_{11}$) were investigated both by simulation and by experiment. Red solid curve: theoretical curve [11], Squares: back-to-back transmission (wavelength used: $\lambda_0$), Triangles: single channel transmission (wavelength used: $\lambda_0$), Circles: best case transmission scenario ($\lambda_0$ for simulation and experiment), Crosses: worst case transmission scenario ($\lambda_1$ and $\lambda_3$ for simulation and experiment, respectively). Blue and green color represents simulation and experimental results, respectively.
In Fig. 4, measurements for the original architecture show that the spread among all eight channels is approximately 1 dB, both in simulation and experiment.

Experimental results in Fig. 5 reveal that there is a spread of 1.2 dB, in terms of required OSNR, among the eight channels of waveband W₁ and W₂ for BER = 10⁻⁹. In close agreement with the experiment, simulation results indicate that there is an OSNR spread of approximately 1.45 dB among the eight channels of wavebands W₁ and W₂. However, simulation also shows that there is a spread of approximately 2 dB between all 16 simulated channels of the optimized architecture for BER = 10⁻⁹. The BER curve for an ideal system [11] is also shown for comparison. For qualitative comparison, experimental eye diagrams are also shown as insets in Figs. 4 and 5, for the best and the worst channels, for both architectures.

Finally, the performance of both architectures is also tested without in-line SOAs, in a back-to-back configuration (see squares in Figs. 4 and 5), as well as for single-channel transmission, after the three selection stages of the optimized configuration (see triangles in Fig. 5). We observe that the penalty difference is negligible among the back-to-back, the single-channel, and the best case transmission scenario (i.e., λ₃₇) for the optimized architecture (see Fig. 5). Similarly, the curves corresponding to the back-to-back and the best case transmission scenario (i.e., λ₅) for the original architecture (see Fig. 4) are indistinguishable.

It is worth noting that the measured performance, in both architectures, is worse than the one predicted by simulation by approximately 1 dB (e.g., compare the back-to-back cases for the simulation and the experiment, respectively). This small difference is attributed to the following parameter mismatch between simulation and experiment: 1) the use of narrower optical filters in the simulation; 2) the use of the same data pattern for modulating all wavelength channels in the experiment, in contrast to the simulation, where each laser is independently modulated with a different bit sequence (a 4 dB degradation is observed using the same data patterns); and 3) the omission of PDG from the SOAs simulation model [13]. Despite this small discrepancy, from Figs. 4 and 5, we can safely conclude that the performance of the optimized architecture is slightly worse than the performance of the original one for the worst channel (whereas, it is identical for best channel). We point out here that the experimental results shown in Figs. 4 and 5 are optimized compared to the ones reports in [9] by 1.4 dB, a penalty found to be due to the low extinction ratio (ER) that holds in the experiment [14]. The ER in [9] was 8 dB, while in this study, the ER was optimized by 5 dB to avoid penalty due to a reduced modulation ER.

In Fig. 6, the OSNR (measured in a resolution bandwidth RB = 0.08 nm) required for BER = 10⁻⁹ for all channels: (a) original and (b) optimized optical interconnect architecture. (Symbols: W₁ = W₄; wavebands used in the optimized architecture; Open and filled circles: simulated and experimental results, respectively).

No FWM [18], [19] products were observed in the recorded spectrum for the specific operating conditions and the wavelengths under test, in the experiment. This indicates that FWM is not a major factor to the observed signal.

From the above, we conclude that the optimized architecture provides a good tradeoff between SOA count reduction and performance degradation. Its relatively small penalty in required OSNR compared to the original architecture justifies its use.

In Section IV-B–D, using simulation, we quantify the contribution of different transmission effects in the performance degradation of both architectures.

**B. Penalty Due to SGM**

As its name indicates, SGM is gain modulation due to instantaneous channel power variation at the SOA input [20]. In this section, we focus on the penalty due to SOA SGM in both optical interconnect architectures under study. To distinguish between the penalty due to SGM and the total system penalty, we perform simulations using a single channel, i.e., the worst and the best channel, in both architectures.

The results for the worst channel are shown in Fig. 7 (red squares). The curves for the ideal system (red line), the back-to-back case (blue circles), and the case of WDM transmission through the interconnect (dash-dotted curve with stars) are also included for comparison. An additional curve
corresponding to the WDM case, obtained by substituting all SOAs and EDFAs by ideal, flat-gain amplifiers, is also shown (black crosses).

Comparing the back-to-back case with the single-channel transmission, we conclude that the penalty is negligible in the original architecture [see Fig. 7(a)] and 1.5 dB in the optimized one [see Fig. 7(b)] at an error probability of $10^{-9}$. In contrast, for the best channels, the penalty is negligible in both architectures (not shown here to avoid clutter). The difference of 1.5 dB in performance between the worst and the best channel of the optimized interconnect is explained as follows: the worst channel reaches higher power levels, due to its allocation closer to the gain peak of the SOAs and, therefore, is more affected by SGM. As expected, SGM is more severe in the optimized architecture than in the original one because the signal passes through one more SOA in the former case.

C. Penalty Due to XGM

SOAs are subject to XGM [21] that results into data pattern-dependent crosstalk among WDM signals when ASK is used [22], [23]. The use of quasi-constant envelope modulation formats, such as return-to-zero (RZ) differential phase-shift keying [15], [22], RZ differential QPSK [16], or PDM-QPSK [8], [9], has been proposed to counteract this effect. We can assess the penalty due to XGM from Fig. 7, by comparing the results for WDM transmission through the optical interconnect after substitution of SOAs and EDFAs by ideal, flat-gain amplifiers.

The penalty due to XGM is negligible for the best channel in both architectures. Plots of the best channel performance are not shown in Fig. 7 to avoid clutter. In contrast, the XGM penalty is equal to 1 dB, for the worst channel of the original architecture [see Fig. 7(a)], and 2 dB, for the worst channel of the optimized architecture [see Fig. 7(b)], respectively.

In the original architecture, the WDM signal bandwidth is smaller so channels are less affected by the SOA gain nonuniformity. More specifically, the eight channels are located uniformly around the SOA’s gain peak and occupy a bandwidth of 800 GHz (see the inset of Fig. 1). In particular, the eight channels exit the first SOA with negligible difference in power. On the other hand, in the optimized architecture, the 16 channels occupy a bandwidth of 2.7 THz (see the inset of Fig. 2) around the SOA’s gain peak, and, consequently, they experience a larger power variation. In addition, power variation as a function of wavelength, due to the gain nonuniformity of the EDFAs and the SOAs, and the insertion loss nonuniformity of the cascaded AWGs exacerbates the power variation among channels. This leads to a different behavior among channels with respect to XGM and to higher penalties compared to the original architecture.

D. Penalty Due to the Concatenation of Optical MUX/DMUXs

AWG MUX/DMUX concatenation leads to narrowing of the optical bandwidth, which, in turn, results in signal attenuation and distortion [10]. In this section, we evaluate, by simulation, the penalty due to the narrowing of the optical bandwidth of the aggregate transfer function of the cascaded AWGs, in both interconnect architectures under study.

We consider conventional AWGs with Gaussian amplitude transfer function and linear phase transfer function. To focus on filter-induced distortion exclusively, we substitute all EDFAs and SOAs, in Figs. 1 and 2, with ideal (flat-gain) amplifiers. In
Assuming that all center frequencies are perfectly aligned to the channel carrier frequency $f_0$, the aggregate transfer function $H_{\text{tot}}(f)$ of the four concatenated AWGs is

$$H_{\text{tot}}(f) = \prod_{i=1}^{4} H_i(f) = A e^{-\frac{1}{2} \left( \frac{f - f_{ci}}{f_{ci}} \right)^2}$$  \hspace{1cm} (2)$$

where $f_c$ is the overall cutoff frequency

$$f_c = \left( \sum_{i=1}^{4} f_{ci}^2 \right)^{-\frac{1}{2}}$$  \hspace{1cm} (3)$$

By substituting $f_{c1} = f_{c2} = 200$ GHz and $f_{c3} = f_{c4} = 20$ GHz, for the cutoff frequencies of the AWG pairs of the discretely tunable Rx in the OSMOSIS optimized interconnect, we find that $f_c \approx 14$ GHz. The equivalent noise bandwidth of the aggregate transfer function is $B_0 = \sqrt{\pi f_c} \approx 25$ GHz [10].

Given that the 95% of the power of an ideal 10 Gb/s NRZ ASK signal occupies 30 GHz [24], we conclude that the signal distortion due to the bandwidth narrowing arising from MUX/DMUX concatenation would be negligible, as indicated by the simulation results shown in Fig. 7(b).

The aforementioned analysis does not take into account the increased filtering of AWG MUX/DMUXs in the presence of spectral broadening due to SPM and XPM in SOAs. This is taken indirectly into account in Fig. 7(a) and (b) (see dash-dotted curves with stars).

V. SUMMARY

In this paper, we assessed the performance of a recently proposed, economically viable, broadcast-and-select, 64 x 64, optical interconnect architecture [7] using a minimum number of SOA-based ON–OFF gates. We compared its performance to its originally proposed counterpart [6], both by experiment and by simulation. We showed that both interconnect architectures perform almost equally well, while the optimized one is advantageous in terms of the number of SOAs required to perform permutation switching.

To examine the impact of SOA nonlinearities and ASE noise accumulation on the performance of the optical interconnect architectures under consideration, each effect was studied separately. The proposed optimized architecture proved to be tolerant in SOA’s nonlinearities. SGM and XGM worsen the performance of the optimized architecture in terms of required OSNR for error-free operation only by about 1 dB for the worst case scenario, when compared to the corresponding performance of the original configuration. FWM and the bandwidth narrowing imparted by the concatenation of AWGs in the architecture proved to have negligible impact on the degradation of the performance of the optimized interconnect.

ASE noise accumulation and WDM channel power variation due to the wavelength-dependent gain of the SOAs affect the performance of the optical interconnect too, resulting both in unequal accumulation of ASE noise for each channel, as well as in channel power variations at the receiver. Finally, we experimentally studied the performance of both optical interconnect architectures. Experimental and theoretical results were in good qualitative agreement.

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**Fig. 8.** Q-factor versus CW laser power (a) for the best and (b) for the worst channel of both the original and the optimized architecture. (Symbols: Red dashed line with circles: WDM transmission in the original architecture, Black dashed line with crosses: WDM transmission in the optimized architecture.)

this way, we neglect all transmission effects related to optical amplifiers.

Plots of BER as a function of OSNR are shown in Fig. 7, for the worst case transmission scenario, for both architectures. Comparing the curve for the back-to-back case to the one for the ideal flat-gain EDFAs, we conclude that this penalty is negligible in both cases. These results can be easily explained by the following analysis.

The Gaussian transfer function of each of the four AWGs is given by the formula

$$H_i(f) = A_i e^{-\frac{1}{2} \left( \frac{f - f_{0i}}{f_{ci}} \right)^2}$$  \hspace{1cm} (1)$$

where $A_i$ is the amplitude, $f_{0i}$ is the center frequency, and $f_{ci}$ is the cutoff frequency of the $i$th AWG ($i = 1, \ldots, 4$).
the SOA input saturation power. From the SOA rate is the normalized optimum threshold, is the sum of average powers of all channels, be the instantaneous SOA gain, , where is the -factor due to the sum of the ASK signals of equal average power at

\[ P_e \approx \frac{1}{2} \left( 1 + 2N_{th}d \right) e^{-2N_{th}d} \]

\[ + \frac{1}{2} \left[ 1 - Q_2(2\sqrt{N_{th}}, 2\sqrt{N_{th}d}) \right] \quad (4) \]

where \( N_{th} \) is the average number of photons at the receiver. The latter is related to the OSNR, calculated in both polarizations, through the equation, OSNR = \( P_s/(2\ln2\Delta\nu \cdot nsp) = N_{th}/2 \). The last equality holds for a resolution bandwidth \( \Delta\nu = 2B_e \), an LPF equivalent noise bandwidth \( B_e = 1/(2T_b) \), where \( T_b \) is the bit period, a spontaneous emission factor \( nsp = 1 \), and an infinite ER. In (4), \( d \) is the normalized optimum threshold, \( 0 \leq d \leq 1 \), and \( Q_m \) is the generalized Marcum’s function [27]

\[ Q_m(a,b) = \int_{b}^{\infty} x \left( \frac{y}{a} \right)^{m-1} e^{-\frac{x^2+y^2}{2}} I_{m-1}(ax) \, dx \]

where \( I_m(x) \) is the \( m \)-th order modified Bessel function of the first kind.

The deterministic semianalytical method [26] for error probability estimation is used in the simulations. When the deterministic approach is used, the BER is calculated from the deterministic signal and statistical properties of the optical, thermal, and shot noises. The module finds the exact (nongaussian) moment generating function (MGF) of the detected signal, taking into account the optical noise spectral shape, relations between the signal and noise polarization states, thermal and shot noises of the receiver and correlations due to postdetection filtering. The bit error rate is then calculated from the MGF using the saddle-point approximation technique [12].

**TABLE I**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Description</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \Gamma )</td>
<td>-</td>
<td>Confinement factor</td>
<td>0.13</td>
</tr>
<tr>
<td>( a_0 )</td>
<td>m²</td>
<td>Differential gain coefficient</td>
<td>5.3 \times 10^{-30}</td>
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<td>( N_{tr} )</td>
<td>m³</td>
<td>Carrier density at transparency</td>
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<td>( d )</td>
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<tr>
<td>( A )</td>
<td>s⁻¹</td>
<td>Linear recombination coefficient</td>
<td>3 \times 10⁸</td>
</tr>
<tr>
<td>( B )</td>
<td>m³ s⁻¹</td>
<td>Bimolecular recombination coefficient</td>
<td>2 \times 10⁻³⁶</td>
</tr>
<tr>
<td>( C )</td>
<td>m⁶ s⁻¹</td>
<td>Auger recombination coefficient</td>
<td>6 \times 10⁻⁴¹</td>
</tr>
</tbody>
</table>

APPENDIX A

Here, we briefly describe the following: 1) the SOA model used in the simulation and its simulation parameters, and 2) the formula used for the error probability for the ideal system.

**A. SOA Model Validation**

For the simulation of the SOAs, the transmission line model (TLM) was used [13]. In the simulation, we assumed that the SOAs in the simulation have 1 mm length and a 90 nm 3 dB gain bandwidth. The other parameters used in the SOA model are extracted by least squares fitting of experimental data for the SOA gain and output power as a function of input SOA power (see Fig. 9) [25]. The most important SOA parameters are shown in Table I.

**APPENDIX B**

Here, using small-signal analysis, we interpret the \( Q \)-factor ceiling observed in Fig. 8, when the launched power per channel is high. We assume \( N \) ASK signals of equal average power at the SOA input. Let \( G \) be the instantaneous SOA gain, \( G_s \) the SOA small-signal gain, \( P_{tot} \) the instantaneous total input power, and \( P_0 \) the SOA input saturation power. From the SOA rate equation for the optical power [28], assuming zero internal loss and constant carrier concentration yields

\[ G = G_s e^{-\frac{g}{G_s}} \]

Assume that the total input power to the SOA is \( P_{tot} = P_0 + \delta P \), where \( P_0 \) is the sum of average powers of all channels and \( \delta P \) is a small perturbation (\( \delta P \ll P_0 \)) due to the sum of the
instantaneous power variation of all channels. Substituting in (6), the amplifier gain is

$$G_0 + \delta G = G_s e^{-\frac{(G_0 + \delta G)(P_0) + \delta P}{P_0}}.$$  

(7)

Expanding the terms in parentheses and ignoring the second-order term $\delta G\delta P$ yields

$$\delta G = -\frac{G_0(G_0 - 1)\delta P}{P_0 + G_0P_0}. \quad (8)$$

The instantaneous power per channel at the output of the SOA amplifier is

$$P_{\text{out}} + \delta P_{\text{out}} = (G_0 + \delta G)(\bar{P} + \delta P), \quad (9)$$

where $\bar{P}$ is the average input power per channel and $\delta P$ is the instantaneous power variation per channel $(\delta P \ll \bar{P})$. Given that $P_{\text{out}} = G_0\bar{P}$ and neglecting $\delta G\delta P$, we get

$$\delta P_{\text{out}} = \bar{P}\delta G + G_0\delta P = \left(-\frac{G_0(G_0 - 1)}{P_0 + G_0P_0}\right)\bar{P}\delta P + G_0\delta P. \quad (10)$$

Because $\delta P$ and $\delta P$ are independent random variables with zero mean value and variances $\sigma^2_{\delta P}$ and $\sigma^2_{\delta P}$, respectively, $\delta P_{\text{out}}$ is also a random variable with zero mean value and variance

$$\sigma^2_{\delta P_{\text{out}}} = \left[-\frac{G_0(G_0 - 1)}{P_0 + G_0P_0}\right] \bar{P}^2 \sigma^2_{\delta P} + G_0^2 \sigma^2_{\delta P}. \quad (11)$$

For each transmitted channel, the instantaneous input power $P_i$ can be explicitly written as

$$P_i = \bar{P} + b_i \Delta \quad (12)$$

where $b_i$ is a binary random variable taking values in the set $\{-1, 1\}$, and $\Delta$ is the fraction of power added to or subtracted from the average input power to yield a logical ONE or ZERO. If $r$ is the ER, defined as $r = (P_{\text{ZERO}})/(P_{\text{ONE}})$ [23], where $P_{\text{ZERO}}$ and $P_{\text{ONE}}$ are the instant powers for the ZEROS and ONES, respectively, $\Delta$ can be expressed as

$$\Delta = \frac{\bar{P}}{1+r}(1-r). \quad (13)$$

The variance of $\delta P$ is

$$\sigma^2_{\delta P} = \bar{P}^2 \left(\frac{1-r}{1+r}\right)^2. \quad (14)$$

Due to channel independence, the variance of the total instantaneous power variation $\delta P$ is

$$\sigma^2_{\delta P} = N \sigma^2_{\delta P}. \quad (15)$$

At the limit $\bar{P} \rightarrow \infty$, the SOA ASE noise is negligible and the OSNR at the output of the SOA is calculated by the formula

$$\text{OSNR} = \frac{\bar{P}_{\text{MNR}}}{\sigma_{\delta P_{\text{out}}}} \quad (16)$$

or, equivalently

$$\text{OSNR} \equiv \frac{G_0}{\left\{\frac{G_0(G_0 - 1)}{G_0NP + P_0}\right\}^{\frac{1}{2}} + \frac{1}{1+r}}. \quad (17)$$

where $G_0 = G_0(P_0) = G_0(N\bar{P})$. It is observed that as $\bar{P} \rightarrow \infty$, the OSNR reaches a ceiling. The same is true for the $Q$-factor given by [14]

$$Q = \frac{\mu_1 - \mu_0}{\sigma_1 + \sigma_0} \quad (18)$$

where

$$\mu_1 = (G_0 + \delta G)(\bar{P} + \delta P)$$

$$\mu_0 = (G_0 - \delta G)(\bar{P} - \delta P)$$

$$\sigma^2_1 = 4(G_0 + \delta G)(\bar{P} + \delta P)hv\Delta v \cdot nsp(G_0 + \delta G - 1)$$

$$\sigma^2_0 = 4(G_0 - \delta G)(\bar{P} - \delta P)hv\Delta v \cdot nsp(G_0 - \delta G - 1). \quad (19)$$

We set

$$G_0 \pm \delta G - 1 \simeq G_0 \pm \delta G \quad (20)$$

which is valid for $G_0 \gg 1$, we use the second-order Taylor series to get

$$(\bar{P} \pm \delta P)^{1/2} = \bar{P} \pm \frac{1}{2} \delta P \quad (21)$$

and we assume that for XGM, the average error probability is equal to the error probability of the innermost traces in the eye diagram corresponding to all ONES and ZEROS [23]. By substitution of (19)–(21) into (18), we get

$$Q \simeq \frac{1}{2\sqrt{a}}\left(\frac{1-r}{1+r}\right)\frac{N\bar{P} + P_0}{G_0(N\bar{P})N\bar{P} + P_0}. \quad (22)$$

where $a = hv\Delta v \cdot nsp$. As $\bar{P} \rightarrow \infty$, $Q$ reaches a ceiling similar to the one observed in Fig. 8 for large-signal modulation which is

$$Q \simeq \frac{1}{2\sqrt{a}}\left(\frac{1-r}{1+r}\right). \quad (23)$$

It is worth noting here that the curves in Fig. 8 do not assume the bell shape shown in [29, Ch. 14, Fig. 15], i.e., the optical interconnect performance does not degrade at high SOA input power levels but reaches a ceiling. This apparent contradiction is due to the fact that, in our simulations, the input power to the photodiode is unlimited, whereas, in practice, there is a maximum optical power that can be received by the photodiode. In [29], there is an attenuator before the photodiode that keeps the optical power below a certain level.

REFERENCES


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