

EE580 – Solar Cells Todd J. Kaiser

- Lecture 03
- Nature of Sunlight

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Wave-Particle Duality

- Light acts as
 - Waves: electromagnetic radiation
 - Refraction - bending of light through a prism
 - Diffraction - bending of light around an edge
 - Interference – adding of light waves
 - Particles: photons – individual packets of energy
 - Photoelectric Effect
 - Blackbody Radiation

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Properties of Light

- Sunlight contains photons of many different frequencies (we see as different colors)
- Visible Light
 - 0.38 microns – 0.77 microns (10^{-6} meters)
 - Blue - Red
- Frequency (f) and Wavelength (λ) are inversely related: $f = 1/\lambda$
 - High Energy \rightarrow High Frequency \rightarrow Short Wavelength
 - Low Energy \rightarrow Low Frequency \rightarrow Long Wavelength

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Electromagnetic Spectrum

Color, wavelength and frequency are interrelated

Color	Wavelength (meters)	Frequency (Hz)
Radio Waves	10^0 to 10^3	10^7 to 10^9
Microwaves	10^{-2} to 10^{-1}	10^{10} to 10^{11}
Infrared	10^{-4} to 10^{-6}	10^{12} to 10^{14}
Visible	$0.38 \mu\text{m}$ to $0.77 \mu\text{m}$	10^{15} to 10^{16}
Ultraviolet	10^{-8} to 10^{-7}	10^{16} to 10^{17}
X Rays	10^{-11} to 10^{-8}	10^{17} to 10^{19}
Gamma Rays	10^{-12} to 10^{-11}	10^{19} to 10^{20}

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Photon Energy

$$E = hf = \frac{hc}{\lambda} \Rightarrow E(eV) = \frac{1.24}{\lambda(\mu)}$$

High energy photon for blue light

Low energy photon for red light

Very low energy photon for infrared (invisible)

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Photon Flux & Energy Density

$$\text{Photon Flux} = \frac{\text{Number of Photons}}{(\text{second})(\text{Area})} = \Phi$$

$$\text{Energy Density} : (\text{Photon Flux})(\text{Energy per Photon}) : H\left(\frac{W}{m^2}\right) = \Phi\left(\frac{hc}{\lambda}(J)\right)$$

For the same intensity of light shorter wavelengths require fewer photons, since the energy content of each individual photon is greater

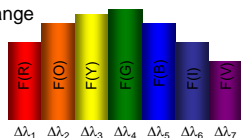
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Radiant Power Density

- The total power density emitted from a light source

$$H = \int_0^{\infty} F(\lambda) d\lambda \Rightarrow \sum_{i=1}^N F(\lambda_i) \Delta\lambda_i$$

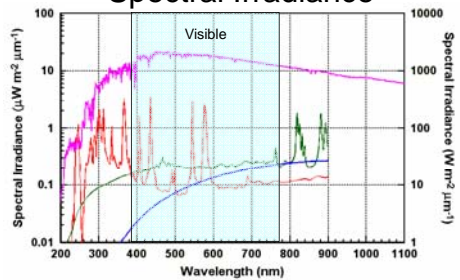
- The spectral irradiance is multiplied by the wavelength range for which it was measured and summed over the measurement range



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Spectral Irradiance



Xenon – (left axis) Sun - (right axis)
Halogen – (left axis)
Mercury – (left axis) Power Density at a particular wavelength

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Solar Radiation

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Blackbody Radiation

- A body in thermal equilibrium emits and absorbs radiation at the same rate
- A body that absorbs all the radiation incident on it is an ideal **blackbody**
- The power per area radiated is given by the **Stefan-Boltzmann Law**

$$H = \sigma T^4$$

- This function has a maximum given by **Wien's Displacement Law**

$$\lambda_{peak} (\mu) = \frac{2900}{T(K)}$$

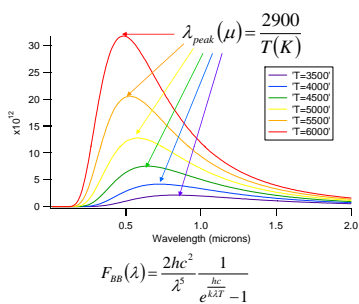
- The spectral irradiance of a blackbody radiator is given by **Planck's Law**

$$F_{BB}(\lambda) = \frac{2hc^2}{\lambda^5} \frac{1}{e^{\frac{hc}{\lambda T}} - 1}$$

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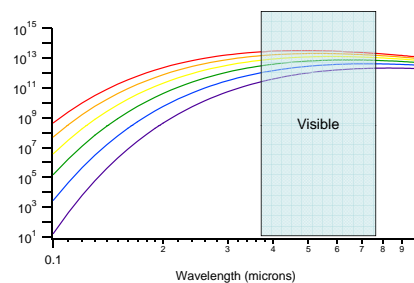
Plot of Planck's Law



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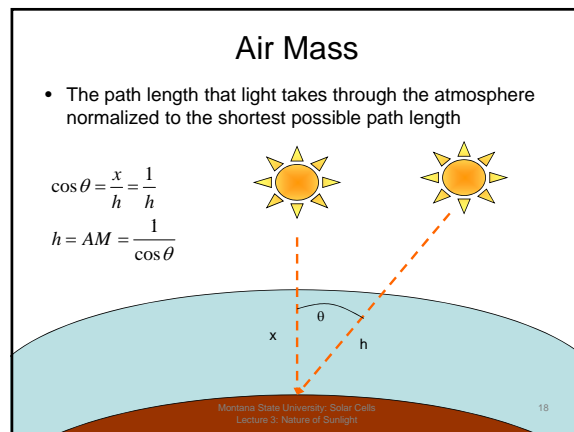
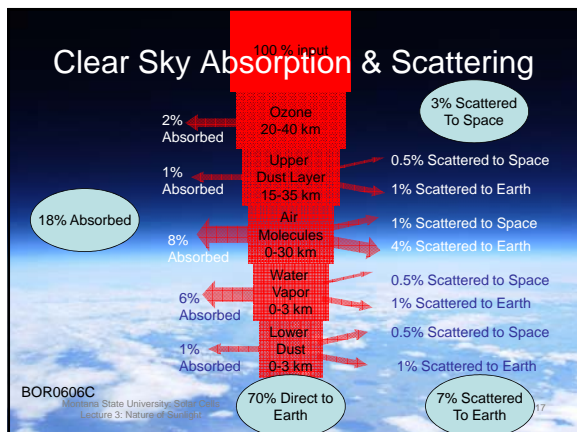
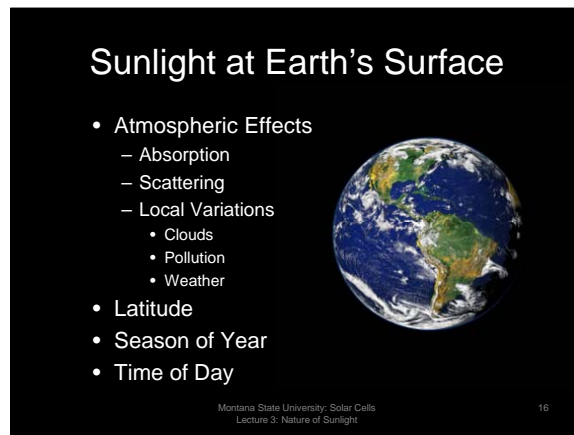
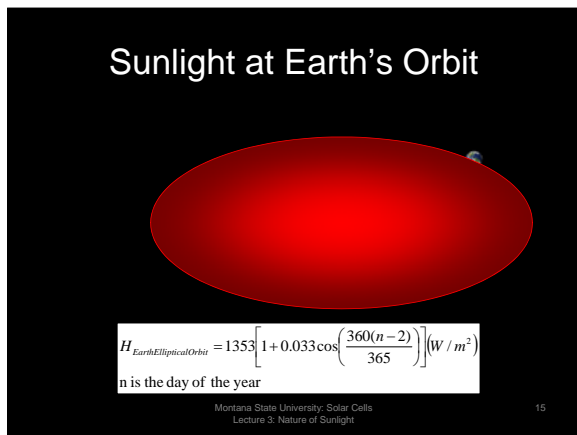
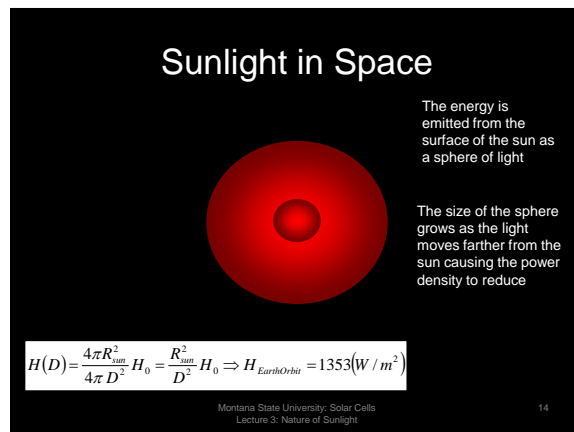
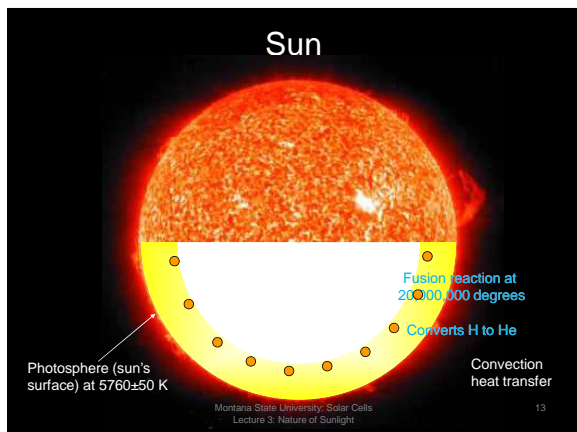
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Sun's maximum at visible spectrum



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Measuring the Air Mass

$\cos \theta = \frac{L}{h} \Rightarrow$
 $AM = \frac{1}{\cos \theta} = \frac{h}{L} = \frac{\sqrt{S^2 + L^2}}{L} = \sqrt{\left(\frac{S}{L}\right)^2 + 1}$

Neglects the curvature of the earth's atmosphere

Object of height (L)
Shadow from object (S)

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EAST SOUTH WEST NORTH

What time of year is this image true?
 March 22: Spring Equinox
 Sept 23: Fall Equinox

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Declination Angle

Mar 23 Declination (δ) = 0°
 Jun 23 Declination (δ) = 23.45°
 Sep 23 Declination (δ) = 0°
 Dec 23 Declination (δ) = -23.45°

$\delta = 23.45^\circ \sin\left[\frac{360}{365}(d - 81)\right]$

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Declination Angle of Sun

North Pole

Summer Solstice $\delta = 23.45^\circ$
 Fall Equinox $\delta = 0^\circ$
 Winter Solstice $\delta = -23.45^\circ$

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Elevation Angle

The elevation angle is the angular height the sun makes with the horizontal

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Polar Plot of Sun Position for Bozeman

Month	6 (0,12) Jan = 1
Day	21 (0,31) Day of the Month
Hour	16 (0,24) Hour in 24-hour time
Min	00 (0,60)
Lat	45 (90,00) S is neg.
Long	-108 (180,180) E is neg.
GMT	+10 (-12,12) hours ahead or behind GMT

Sun's Position Throughout the Day

Day Number	172 days
Eqn of Time	-1.45 minutes
LSTM	-150.00 minutes
Time Corr.	38.55 minutes
L. Sol. Time	16:51 hour:mins
Hour Angle	165.00 deg.
Declination	23.45 deg.
Sunrise	07:39 hour:mins
Sunset	08:58 hour:mins
Azimuth	208.19 deg.
Altitude	34.44 deg.

Summer
Spring/Fall
Winter

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